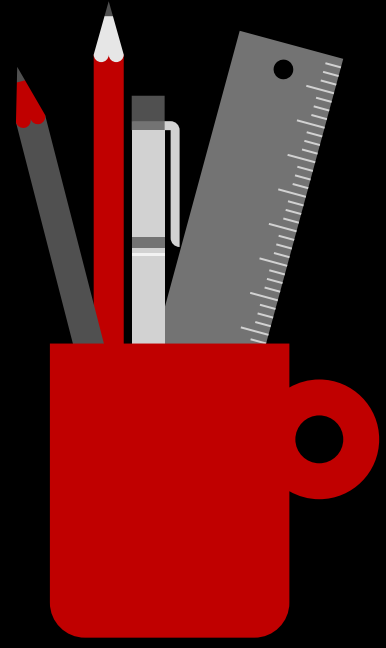


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$$i) \log_a mn = \log_a m + \log_a n$$

$$\text{Let } \log_a m = x, \quad \log_a n = y$$

$$a^x = m, \quad a^y = n$$

$$m \cdot n = a^x \cdot a^y$$

$$mn = a^{x+y}$$

$$\log_a mn = x + y$$

$$\log_a mn = \log_a m + \log_a n$$



$$\text{ii) } \log_a \frac{m}{n} = \log_a m - \log_a n$$

Let $\log_a m = x$, $\log_a n = y$

$$a^x = m$$

$$a^y = n$$

$$\frac{m}{n} = \frac{a^x}{a^y}$$

$$\frac{m}{n} = a^{x-y}$$

$$\log_a \frac{m}{n} = x - y$$
$$\log_a \frac{m}{n} = \log_a m - \log_a n$$



$$3) \log_a m^n = n \log_a m$$

Let $\log_a m = x$

$$a^x = m$$

$$m^n = a^{nx}$$

$$\log_a m^n = nx$$

$$\log_a m^n = n \log_a m$$



$$4) \log_a n = \log_b n \times \log_a b \quad \text{or} \quad \frac{\log_b n}{\log_b a}$$

Let $\log_b n = x$

$$b^x = n$$

taking log of both sides

$$\log_a b^x = \log_a n$$
$$x \cdot \log_a b = \log_a n$$

$$\log_a n = \log_b n \times \log_a b$$

put $n = a$

$$\log_a a = \log_b a \times \log_a b$$

$$1 = \log_b a \times \log_a b$$

$$\log_a b = \frac{1}{\log_b a}$$



$$\log_a^n \log_a^b = \frac{1}{\log_b^a}$$

$$\therefore \log_a^n = \log_b^n \times \log_a^b$$

$$\therefore \log_a^b = \frac{\log_b^n}{\log_b^n}$$

$$\frac{\log_a^n}{\log_b^n} = \frac{1}{\log_b^a}$$

$$\log_a^n = \frac{\log_b^n}{\log_b^a}$$